

**Τράπεζα Θεμάτων (ΙΕΠ)
Γεωμετρία Β΄ Λυκείου**

Εκφωνήσεις



2025-2026

Ασκησόπολις

Στέλιος Μιχαήλογλου / Δημήτρης Πατσιμάς / Νίκος Τούντας

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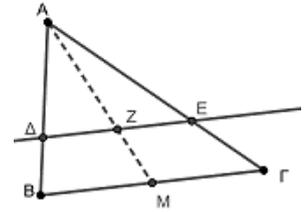


Τα θέματα προέρχονται από την πλατφόρμα της Τράπεζας Θεμάτων Διαβαθμισμένης Δυσκολίας που αναπτύχθηκε (MIS5070818-Τράπεζα θεμάτων Διαβαθμισμένης Δυσκολίας για τη Δευτεροβάθμια Εκπαίδευση, Γενικό Λύκειο-ΕΠΑΛ) και είναι διαδικτυακά στο δικτυακό τόπο του Ινστιτούτου Εκπαιδευτικής Πολιτικής (Ι.Ε.Π.) στη διεύθυνση (<http://iep.edu.gr/el/trapeza-thematon-arxiki-selida>)

Αναλογίες

Θεώρημα Θαλή 2^ο Θέμα

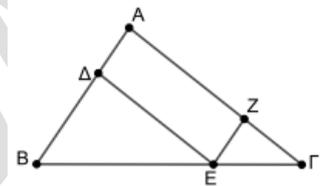
14534. Θεωρούμε τρίγωνο $AB\Gamma$ με $AB=6$ και $A\Gamma=9$. AM είναι η διάμεσος του τριγώνου και το σημείο Z εσωτερικό στην AM ώστε να σχηματίζει λόγο $\frac{AZ}{AM} = \frac{2}{3}$. Από το σημείο Z φέρουμε ευθεία παράλληλη στην πλευρά $B\Gamma$, που τέμνει τις πλευρές AB και $A\Gamma$ στα σημεία Δ και E αντίστοιχα.



α) Να αποδείξετε ότι $\frac{A\Delta}{AB} = \frac{2}{3}$ και $\frac{AE}{E\Gamma} = 2$.

β) Να υπολογίσετε τα μήκη των τμημάτων $A\Delta$ και ΓE .

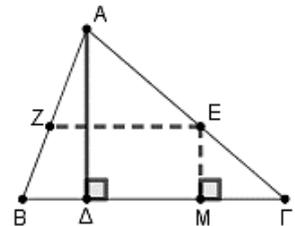
14579. Δίνεται το τρίγωνο $AB\Gamma$ και τα σημεία Δ , E και Z των πλευρών του AB , $B\Gamma$ και $A\Gamma$ αντίστοιχα, ώστε η ΔE να είναι παράλληλη στην $A\Gamma$. Επίσης $AB = 3A\Delta$.



α) Να βρείτε τους λόγους $\frac{B\Delta}{A\Delta}$ και $\frac{BE}{E\Gamma}$.

β) Αν επιπλέον γνωρίζετε ότι $A\Gamma = 3,9$ και $\Gamma Z = 1,3$ να αποδείξετε ότι η $Z E$ είναι παράλληλη της AB .

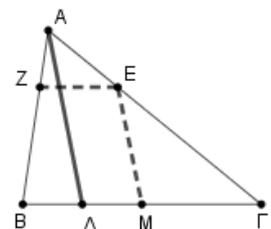
15830. Στο τρίγωνο $AB\Gamma$ του διπλανού σχήματος, το $A\Delta$ είναι ύψος του τριγώνου. Η κάθετος στην πλευρά $B\Gamma$ σε ένα άλλο σημείο της M τέμνει την $A\Gamma$ στο E . Από το E φέρνουμε παράλληλη στην $B\Gamma$, που τέμνει την AB στο Z . Να αποδείξετε ότι:



α) $\frac{ZA}{ZB} = \frac{EA}{E\Gamma}$

β) $\frac{ZA}{ZB} = \frac{M\Delta}{M\Gamma}$

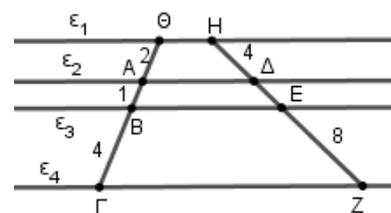
15831. Στο τρίγωνο $AB\Gamma$ του παρακάτω σχήματος, το M είναι μέσο της πλευράς $B\Gamma$ και το Δ είναι το μέσο του MB . Από το M φέρνουμε παράλληλη στην $A\Delta$, που τέμνει την $A\Gamma$ στο E . Από το E φέρνουμε παράλληλη στην $B\Gamma$, που τέμνει την AB στο Z . Να αποδείξετε ότι:



α) $\frac{EA}{E\Gamma} = \frac{1}{2}$

β) $\frac{ZA}{ZB} = \frac{1}{2}$

21987. Οι ευθείες $\Gamma\Theta$ και ZH τέμνουν τις παράλληλες ευθείες ϵ_1 , ϵ_2 και ϵ_3 στα σημεία Θ , A , B και H , Δ , E αντίστοιχα και την ευθεία ϵ_4 στα σημεία Γ και Z όπως στο παρακάτω σχήμα. Επίσης δίνονται τα μήκη $\Theta A = 2$, $AB = 1$, $B\Gamma = H\Delta = 4$ και $E Z = 8$.

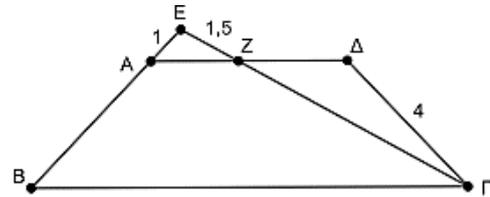


α) Να αποδείξετε ότι $\Delta E = 2$.

β) Να αποδείξετε ότι η ευθεία ϵ_4 είναι παράλληλη στις ευθείες ϵ_1 , ϵ_2 και ϵ_3 .

γ) Να σχεδιάσετε το ευθύγραμμο τμήμα ΘZ το οποίο τέμνει την ευθεία ε_2 στο K και την ευθεία ε_3 στο Λ και να υπολογίσετε τον λόγο $\frac{\Lambda Z}{K\Lambda}$.

22132. Δίνεται ισοσκελές τραπέζιο $AB\Gamma\Delta$ με $AB = \Gamma\Delta = 4$ και με βάσεις $A\Delta$ και $B\Gamma$. Στην προέκταση της πλευράς BA προς το A παίρνουμε σημείο E , ώστε $EA = 1$. Το ευθύγραμμο τμήμα $E\Gamma$ τέμνει την $A\Delta$ στο σημείο Z και $EZ = 1,5$.



α) Να αποδείξετε ότι $Z\Gamma = 1,5AB$.

β) Να υπολογίσετε το μήκος του $Z\Gamma$.

γ) Αν επιπλέον $B\Gamma = 10$, να υπολογίσετε το μήκος της πλευράς AZ του τριγώνου EAZ .

μ
2 μ

14535.

$\hat{A} = 48^\circ, Z\Delta = 12, ZE = 20 \quad \hat{Z} = 48^\circ.$

)

i.

ii.

$\mu : = 9, = 15$

14536.

$\hat{Z} = 66^\circ \quad AB = 3 \cdot E\Delta.$

)

i.

ii.

14537.

$\hat{A} = 48^\circ, \hat{B} = 53^\circ, \hat{E} = 79^\circ$ και $\hat{Z} = 48^\circ.$

)

i.

ii.

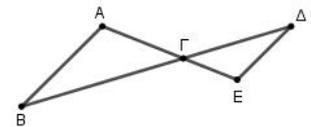
14538.

$\mu \mu$

)

i.

ii.



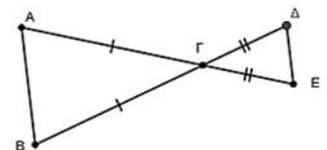
14546.

μ

)

i.

ii.



16100.

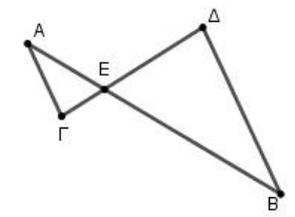
$= 4, = 2, = 6, = 15 \quad = 5, = 12.$
 $\frac{B\Delta}{A\Gamma}, \frac{\Delta E}{E\Gamma}, \frac{BE}{AE}.$

)

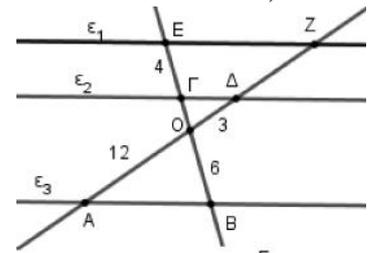
)

)

$\hat{A} = \dots\dots, \hat{\Gamma} = \dots\dots, \angle \hat{E}\Gamma = \dots\dots$

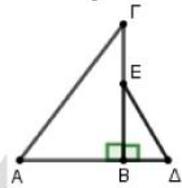


16086. = 3, = 12, = 6. 1, 2 3 . = 4,
) μ μ .
)

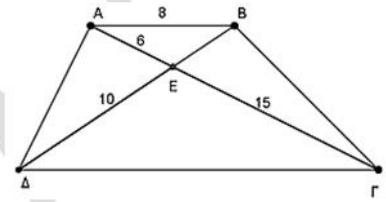


) = 1.5 = 8, $\frac{EZ}{AB}$.

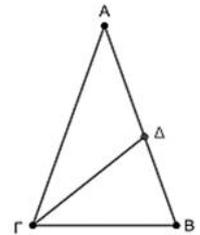
16099. = 36, = 16 = 24. $\hat{A} = \hat{\Delta}$,
) μ .
)



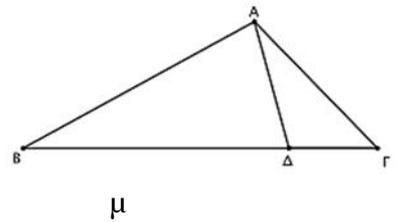
16113. , = 6, = 8, = 15 // , μ μ
) μ .
) μ .
) μ μ .



16126. = 24. μ = 36
) μ = 16. μ μ
 μ $\frac{3}{2}$. μ μ
) μ μ μ μ .

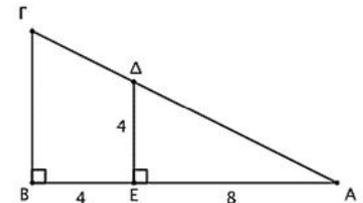


16755. μ = 2 μ .
) = 2 , μ .
) $\frac{B\Gamma}{A\Gamma}$ και $\frac{A\Gamma}{\Gamma\Delta}$.
) μ .

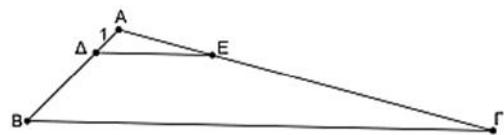


$\hat{B}\hat{A}\hat{\Gamma} = \dots\dots\dots$, $\hat{B} = \dots\dots\dots$

21350. μ $\hat{B} = \hat{E} = 90^\circ$,
 = 8, = 4 = 4.
) μ .
) μ .
) μ .



21986. μ μ
 = 1, μ .
) . = .
) = = 9:
 i. = 3 = 4.
 ii.



2 μ

14549. μ , , : =7, =3 =5.

) μ . μ

14600.) μ

6, 5, $\sqrt{37}$.

) μ =6, =5 = $\sqrt{37}$. μ

14620. μ =20 =8.

) > : μ μ .

) =4, μ μ .

14627. μμ μ AB = $3\sqrt{2}$ και AΔ = 3.

) ΔE = ZB = $\sqrt{3}$.

) = = .

16080. μ = 5, BΓ = $\sqrt{41}$ = 8.

) = 3, μ μ . μ

16101. = 8, = 6 = 11.

) μ . μ

16804. ο μ : μ μ μ μ

i. μ μ μ μ

ii. μ μ μ μ

iii. μ μ μ μ

iv. μ μ μ μ

v. $AG^2 = AB^2 + \dots - 2B\Gamma \cdot \dots$

vi. $B\Gamma^2 = \dots + AG^2 - 2\dots \cdot A\Theta$

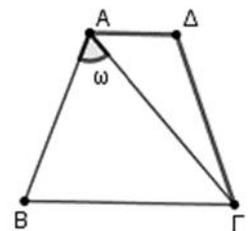
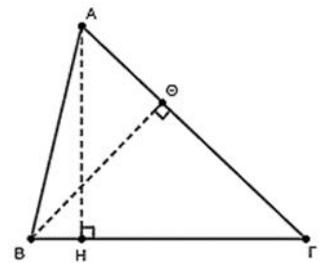
) = 4, = 5 = 6, μ μ μ μ .

17343. μ = 3,

= = 5, = 8 $\hat{A} = 120^\circ$.

) = 7.

) $\text{cosec } \omega = \frac{1}{7}$, \hat{BAG} .



$$\cos 120^\circ = -\frac{1}{2}$$

17354.

) μ

i.

ii.

iii. $\mu \mu$

.....

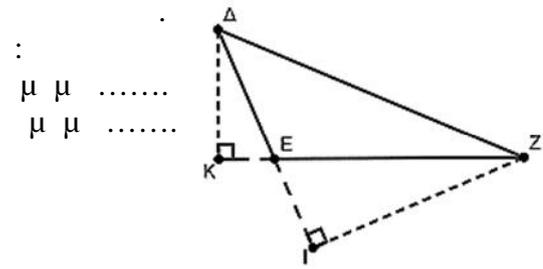
iv. $\mu \mu$

.....

v. $\Delta Z^2 = \Delta E^2 + \dots + 2EZ \cdot \dots$

vi. $EZ^2 = \dots + \Delta Z^2 - 2 \dots \cdot \Delta I$

) $= 2, = 4 = 5,$



21302.

) $= 4.$

) $AG = \sqrt{80}.$

)

22248.

)

)

)

)

)

)

i.

ii.

22512.

)

)

)

29786.

)

)

)

)

)

)

)

)

)

)

)

)

)

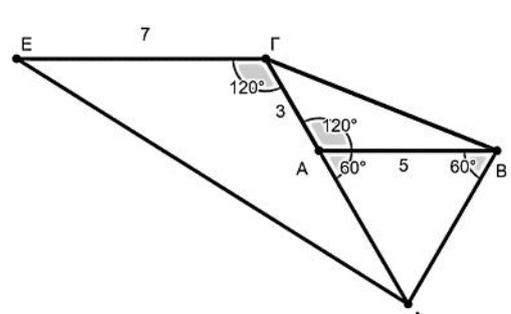
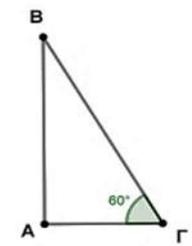
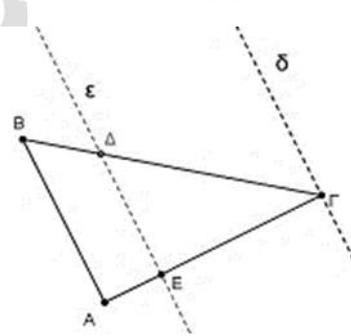
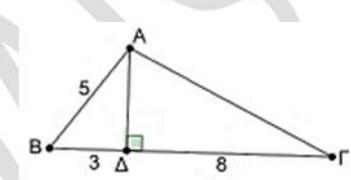
)

)

)

)

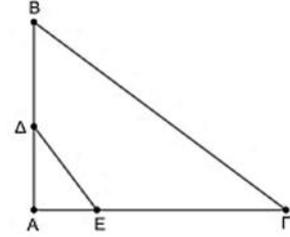
)



4 μ

22400.

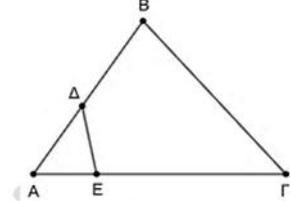
$\mu = 9, \mu = 12, \mu = 4, \mu = 3,$
 $\mu = 15 (\mu = 1).$
 i.
 ii. $\mu = 5.$



Σχήμα 1

$\mu = 10, (\mu = 2).$

i.
 ii. $\Delta E = \frac{10}{3}.$



Σχήμα 2

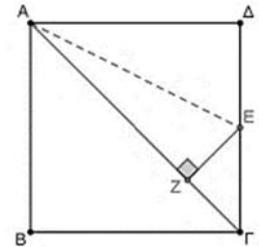
21185.

$\mu = 5, 4, 3$
 $\mu = 10, 8, 6.$

3 μ

21102.

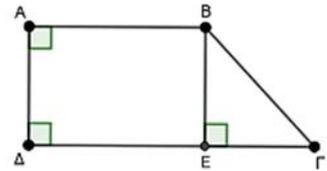
i. $AG = \alpha\sqrt{2}.$
 ii. $AE = \alpha\frac{\sqrt{3}}{2}.$



21823.

$\hat{A} = \hat{\Delta} = 90^\circ$, $\mu = 4$, $\mu = 5$, $\mu = 8$.

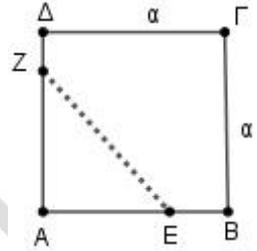
) μ , μ , μ .
) μ , μ .
) μ : $\frac{(B\Delta\Gamma)}{(AB\Gamma\Delta)}$.



16821.

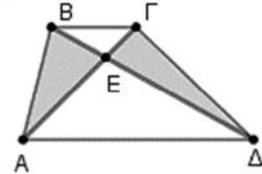
$AE = \frac{3}{5}AB$
 $AZ = \frac{4}{5}A\Delta$.

) μ , μ .
) μ , μ .
) μ , μ .



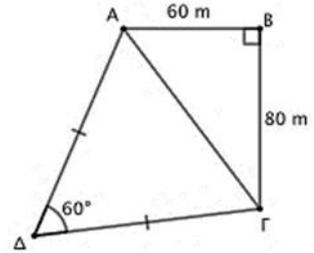
22032.

) μ (//) μ .
) μ , μ .
) μ , μ .



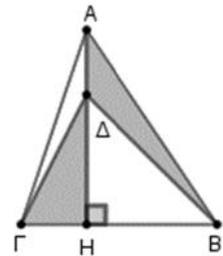
22035.

) μ , μ = 60 m , μ = 80 m , $\hat{A} = 60^\circ$ = .
) μ .
) μ , μ ;



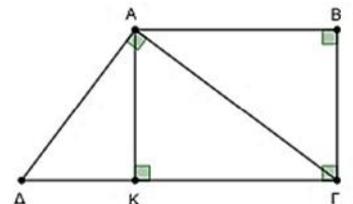
22331.

) μ = 20 , μ = 12 , μ = 5 , μ = 16 .
) μ = 4 .
) μ () = 24 .



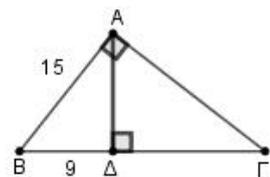
22338.

) μ $\hat{B} = \hat{\Gamma} = 90^\circ$.
) μ = 12 , μ = 9 , μ = 16 .
) μ .



22339.

) μ $\hat{A} = 90^\circ$.
) μ = 9 .
) μ : μ .
 i. μ = 25 , μ .
 ii. μ = 20 .



22104.

) :

i. $(ABM) = \frac{1}{2}(AB\Delta)$.

ii. $(ABM) + (M\Delta\Gamma) = \frac{1}{2}(AB\Gamma)$.

)

22396.

= 3 = 2.

i. = 4.

ii. () = 10.

)

i. μ
ii. μ

22509.

= 2 = . = x

, x $N = 2x$, 2 , 2 .

)

)

)

)

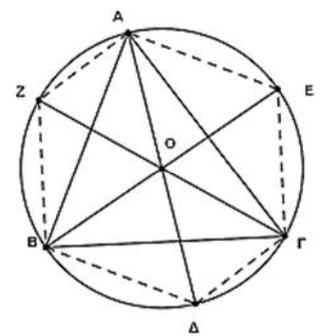
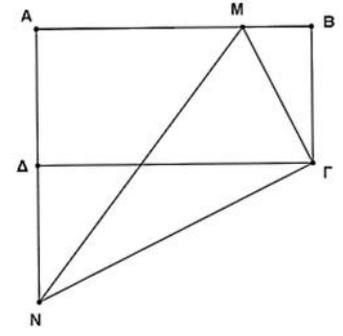
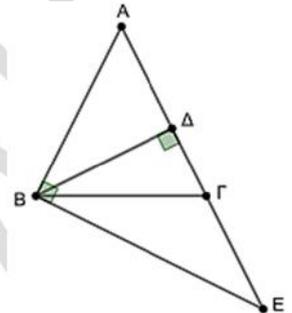
22510.

μ μ , μμ

) () = () () = ()

) () = () + () - ()

) () = 2()



3 μ

17908. μ = 4, β = √17 = 5.
)
)
i.
ii. μ .

Ασκησότητες

2 μ

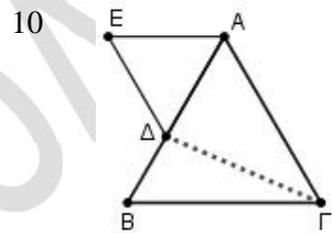
15979. $\mu = 5 \quad \hat{A} = 120^\circ$:
) $B\Gamma = 5\sqrt{3}$) $(AB\Gamma) = \frac{25\sqrt{3}}{4}$

17346. $\mu = 6, \quad = 4 \quad \hat{B} = 60^\circ$.
) $A\Gamma = 2\sqrt{7}$.

)
) $\eta\mu 60^\circ = \frac{\sqrt{3}}{2}$ και $\sigma\upsilon\nu 60^\circ = \frac{1}{2}$.

17347. $\mu = 10$ 6.

) $(A\Gamma\Delta) = 15\sqrt{3}$.
)
 ($\eta\mu 60^\circ = \frac{\sqrt{3}}{2}$

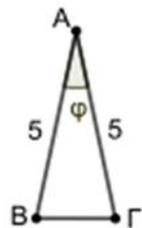


21196. $\mu = 8 \quad = 6$.
) $\mu = 24$.

)
 i. μ
 ii. v_α
 iii. $\mu\mu$

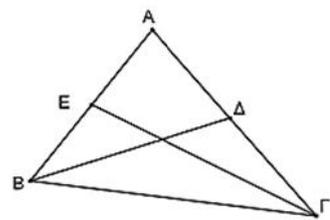
21299. $\mu = 5$
 $\eta\mu\phi = \frac{2}{5}$.

) μ
) B μ

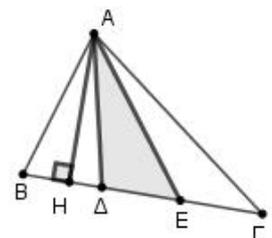


21838. $\mu = 8, \quad = 12$
 $\hat{A} = 60^\circ$.

) μ
) $(AB\Gamma) = 24\sqrt{3}$.
) μ
 i. μ
 ii. $\mu \mu (EB\Gamma) = (\Delta\Gamma B) = 12\sqrt{3}$.



22259. $= =$, μ , μ ,



) $(\Delta \Lambda \text{E}) = \frac{1}{3}(\text{AB}\Gamma).$

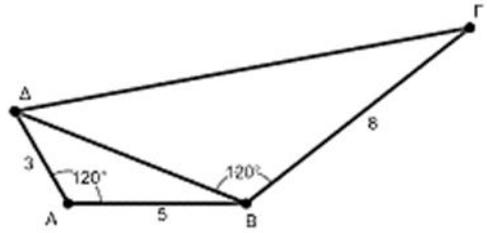
) μ , $(\text{AM}\text{E}) = \frac{1}{6}(\text{AB}\Gamma).$

22511. μ = 2, = 3 $\hat{\text{A}} = 60^\circ$:

-) μ
-) μ
-) .

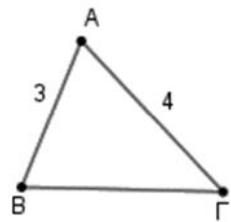
29784. μ μ

- $\hat{\text{A}} = 120^\circ$ = 5, = 8, = 3
-) μ $\hat{\text{A}} = 120^\circ$ 7 μ
-) μ
-) μ



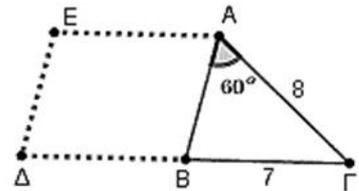
22101.

- μ 3 4
-) $\hat{\text{A}} = 60^\circ$:
- i. μ
- ii. μ
-) μ μ ; μ μ



22369. μ = 8,

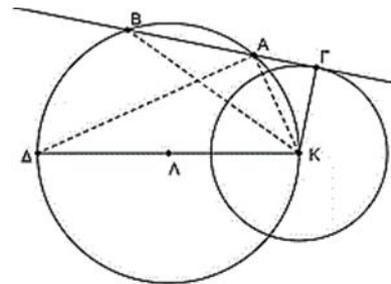
- $\hat{\text{A}} = 60^\circ$ = 7 = 3 = 5.
-)
-) μ .



- i. = 5.
- ii. μ $(\text{AB}\Gamma) = 10\sqrt{3}$.
- iii. μ μ μ = μ μ μ

22568.

- R=10, μ = 6. μ
- (,) μ (, R)
- μ (, R) μ
-) :
- i. μ ii. = 120
-) = 15, μ



3 μ

21783.

, μ $\hat{\Gamma} = 90^\circ$, $\hat{A} = 30^\circ$

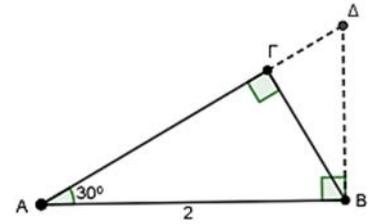
= 2.

) $A\Gamma = \sqrt{3}$.

) μ , μ , μ

$A\Delta = \frac{4\sqrt{3}}{3}$.

) μ , $(KAB) = \frac{\sqrt{3}}{3}$.



29849.

= 6 = 8.

)

)

)

i.

ρ

μμ

ii.

R

μμ

Ασκησολογία

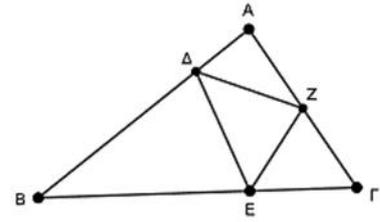
2 μ

15978.

$\Delta\Delta = \frac{1}{4} AB$, $BE = \frac{2}{3} B\Gamma$ $\Gamma Z = \frac{1}{2} A\Gamma$.

i) $(\Delta\Delta Z) = \frac{1}{8}(AB\Gamma)$, $(BE\Delta) = \frac{1}{2}(AB\Gamma)$, $(\Gamma EZ) = \frac{1}{6}(AB\Gamma)$.

ii) $(\Delta EZ) = \frac{5}{24}(AB\Gamma)$



16127.

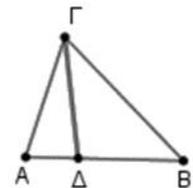
i) $\mu = 9$ $\mu = 8$.

ii) $\mu = 6$.

16756.

i) $\frac{(AB\Gamma)}{(\Delta B\Gamma)} = \frac{AB}{\Delta B}$.

ii) $(\Delta B\Gamma) = 25$ $\mu = 5$.



16770.

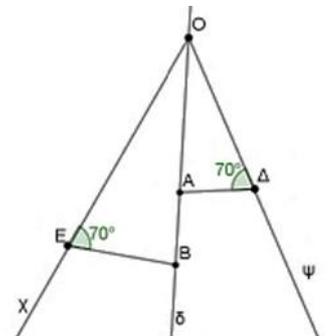
$\hat{\chi O\psi}$ μ μ μ μ .

$\hat{O\epsilon B} = 70^\circ$ μ .

$\hat{O\Delta A} = 70^\circ$.

i) $\frac{OA}{OB} = \frac{2}{3}$.

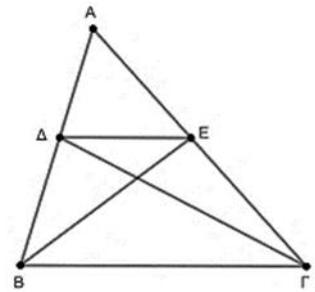
ii) $\mu = 28$ μ .



16806.

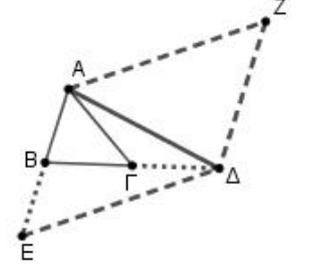
i) $\frac{(A\Delta E)}{(\Delta EB)} = \frac{A\Delta}{\Delta B}$ $\frac{(A\Delta E)}{(\Delta E\Gamma)} = \frac{AE}{E\Gamma}$.

ii) $(\Delta EB) = (\Delta E\Gamma)$.



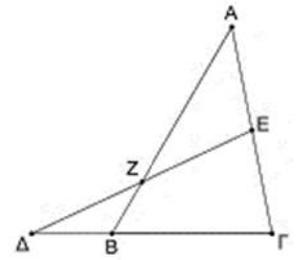
18561.

$\mu = 25 \text{ m}^2$, $\mu = 50 \text{ m}^2$.



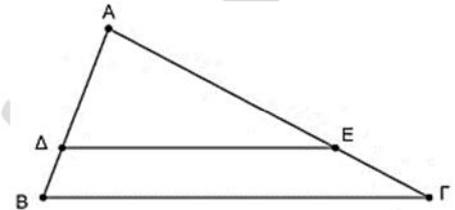
20667.

-) $(AB\Gamma) = 4A\Gamma \cdot \eta\mu\Gamma.$
-) $(\Gamma\Delta E) = 3A\Gamma \cdot \eta\mu\Gamma.$
-) $12 \mu.$



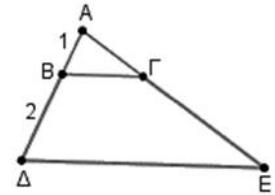
21120.

- i. $AB = \sqrt{2}.$
- ii. $2,$



21304.

-) $1/3.$
-) $8,5,$
-) $15,$



21636.

- i. $\lambda = \frac{3}{4}.$
- ii. $\frac{(AB\Delta)}{(A\Gamma\Delta)}.$

22070.

- i. $\frac{(AB\Delta)}{(A\Gamma\Delta)}.$

4 μ

16114.

μ

$$\Gamma E = \frac{1}{4} \Gamma A.$$

) μ $A\Delta = \frac{1}{3} AB:$

i. () = 4().

ii. μ ,

$$\frac{EZ}{\Gamma H}.$$

) μ () = 2().

16582.

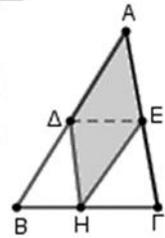
μ

) $\frac{A\Delta}{AB} = \frac{AE}{\Gamma\Gamma} = \frac{1}{2}.$

i. μ $\frac{1}{4}$

ii. μ μ μ μ μ μ

) $\frac{A\Delta}{AB} = \frac{AE}{\Gamma\Gamma} = \lambda,$ μ



16732.

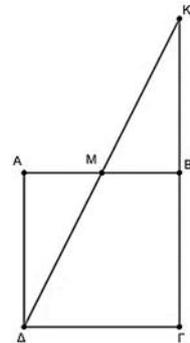
μ

) μ

) $(MKB) = \frac{1}{4} (\Delta K\Gamma).$

) $(MB\Gamma\Delta) = \frac{3}{4} (AB\Gamma\Delta).$

) () = 75 m²



17907.

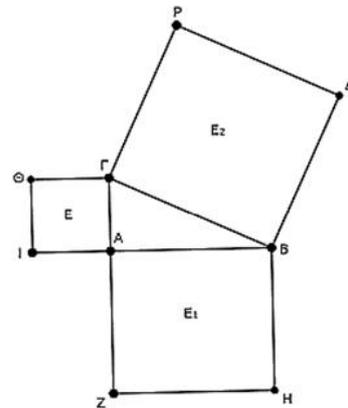
Z, μ , 1, 2, μ

$1 = 4, 2 = 5 :$

) μ

) μ , ,

) =1 μ



17956.

) $(EK\Delta) = \frac{(BE\Delta)}{2}$.

) $(EZ\Delta) = \frac{(AE\Delta Z)}{2}$.

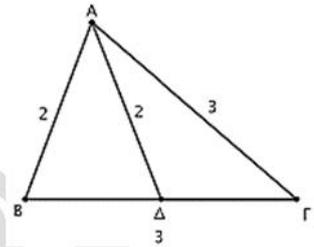
18101.

$= 3$ $= 2$.

) \hat{B} και $B\hat{A}\Gamma$

)

) $\frac{(AB\Gamma)}{(B\Delta A)}$ μ



18301.

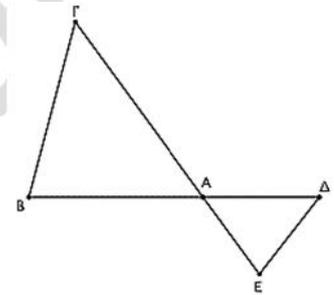
) $A\Delta = \frac{1}{2} AB$ και $AE = \frac{2}{5} A\Gamma$,

$\frac{(A\Delta E)}{(AB\Gamma)}$.

) $A\Delta = \frac{1}{\lambda} AB$ και $AE = \frac{\lambda}{\mu} A\Gamma$, μ

) $\frac{(A\Delta E)}{(AB\Gamma)}$

) μ « () = () ».



18302.

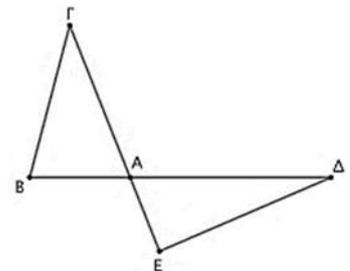
) $= 2$ $AE = \frac{1}{2} A\Gamma$,

)

$= \mu \cdot$ $=$ μ , μ μ μ μ

) $A\Gamma = \frac{3}{2} AB$ $= 2$,

μ .



18369.

$\mu = , \hat{A} = 36^\circ .$

)

$\mu , :$

i.

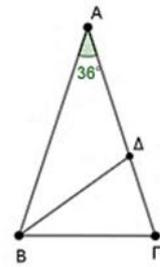
$\mu .$

ii.

)

$\mu \mu .$

$\frac{(\Delta B \Delta)}{(\Delta B \Gamma)} = 3 .$



18370.

$\mu \mu = 2 .$

)

$\mu \mu \mu \mu \mu \mu .$

)

$= 2 \quad M\Gamma = 2\sqrt{2}p .$

i.

$\frac{MO}{M\Gamma} = \frac{M\Delta}{MA} .$

ii.

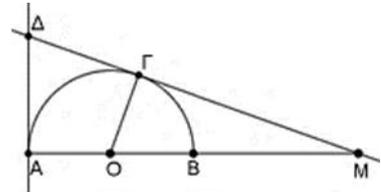
$BM = \lambda \cdot p ,$

$\mu ,$

μ

,

$() = 9() .$



18371.

$\mu \mu$

$\mu . \mu$

i.

$\frac{(\Delta E \Gamma)}{(\Delta B \Gamma)} = \frac{\Delta E}{2B\Gamma} .$

ii.

$() = () .$

)

$\frac{(\Delta E \Gamma)}{(\Delta B \Gamma)}$

$\hat{\Delta} = \hat{\Gamma} ,$

$\frac{\Delta \Gamma}{\Delta \Gamma} = \frac{\Delta E}{AB} = \frac{1}{2} .$

μ

$\hat{\Delta}, \hat{\Gamma}$

$\mu . \mu ,$

μ

$\frac{(\Delta E \Gamma)}{(\Delta B \Gamma)} = \left(\frac{\Delta E}{AB} \right)^2 = \left(\frac{1}{2} \right)^2 = \frac{1}{4} .$

μ

$\mu \mu$

$\mu ;$

20678.

)

)

)

)

)

)

)

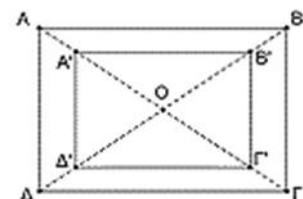
)

)

i.

μ

$40 \text{ cm} \quad \hat{A\hat{O}B} = 120^\circ .$



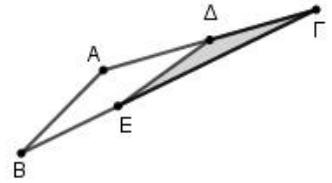
) μ

22260.

$\hat{A} = 150^\circ$.

$GE = \frac{2}{3}GB$,

$\eta\mu 150^\circ = \frac{1}{2}$.



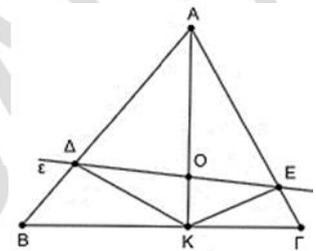
) μ

$\frac{(ΓΔΕ)}{(ΑΒΓ)}$

) μ

22340.

$AO = \frac{3}{4}AK$.



) μ :

i. $(AOΔ) = \frac{3}{4}(AKΔ)$.

ii. $(AOE) = \frac{3}{4}(AKE)$.

iii. $(AΔE) = \frac{3}{4}(AΔKE)$.

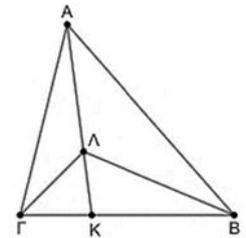
) $(AΔE) = \frac{3}{4}(ΑΒΓ)$;

22375.

$= 2$

$= 2$ E_1, E_2, E_3 και E_4 μ

$μ μ$



) μ :

i. $\frac{E_1}{E_2} = 2$ και $\frac{E_4}{E_3} = 2$.

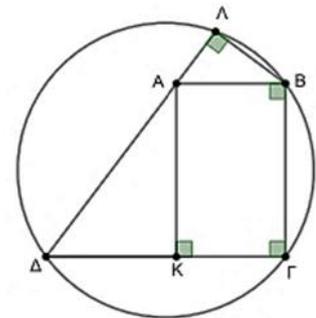
ii. $E_1 = E_3$.

) $E_1 = 10$, μ AB .

22380.

$= 16$, $= 22$ $= 20$.

$\hat{B} = \hat{\Gamma} = 90^\circ$



) μ :

i. $= 12$,

ii. μ 96 .

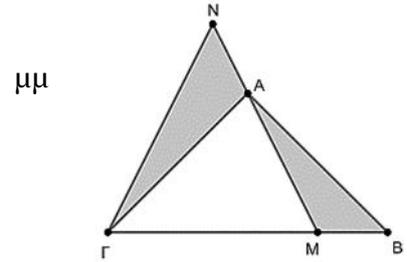
) μ

) μ μ μ μ μ

22404.

$$\frac{MB}{MG}$$

$$\frac{NA}{NM}$$



μ μ

) $\frac{MB}{MG} = \frac{1}{3}$ $\frac{NA}{NM} = \frac{1}{4}$.

i. $\frac{(AMB)}{(AMΓ)} = \frac{1}{3}$. ii. $\frac{NA}{AM} = \frac{1}{3}$. iii. () = ().

) $\frac{MB}{MG} = 1$ () = ().

$$\frac{NA}{NM}$$

μμ μ μ .

22406.

$$= 2$$

μ

)

μ

)

μ

)

$$= 12 \quad \eta\mu B = \frac{3}{4}$$

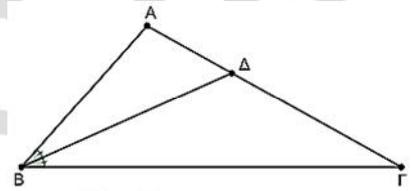
i.

μ

108.

ii.

μ



22407.

μ

μ

$$= 10, \quad = 15 \quad = 9.$$

)

:

i. $= 12$ () = 60.

ii. () = 24 () = 36.

)

μ

i.

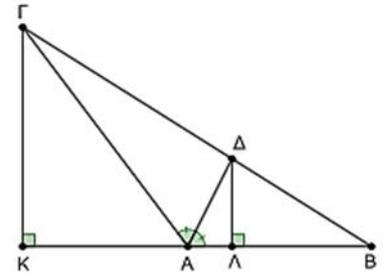
$$\frac{\Delta\Lambda}{\Gamma\text{K}} = \frac{2}{5}$$

ii.

$$\frac{\Lambda\text{B}}{\Lambda\text{K}}$$

μ

μμ μ μ .



3 μ

19037. μ μ , , , ,

$$\Delta B = \frac{1}{5} AB, \quad E\Gamma = \frac{1}{4} B\Gamma, \quad Z\Gamma = \frac{1}{2} A\Gamma.$$

$$\frac{(\Delta BE)}{(\Delta B\Gamma)}, \quad \frac{(E\Gamma Z)}{(\Delta B\Gamma)}, \quad \frac{(Z\Delta\Delta)}{(\Delta B\Gamma)}.$$

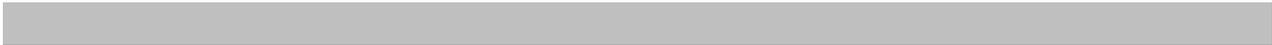
$$\frac{(\Delta BE)}{(\Delta B\Gamma)} = 120, \quad \mu .$$

29850. = = 5 = 6 .

$$\mu .$$

$$\mu \mu = 10.$$

$$\mu .$$



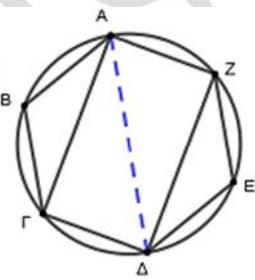
2 μ

20638.

v_1 και v_2 , ω_1 και ω_2
 φ_1 και φ_2 , v_1 v_2 $\mu \frac{1}{2}$, ω_1 και ω_2
) ω_1 και ω_2
) $v_1 = 5$,
 $\frac{\varphi_1}{\varphi_2}$.

21841.

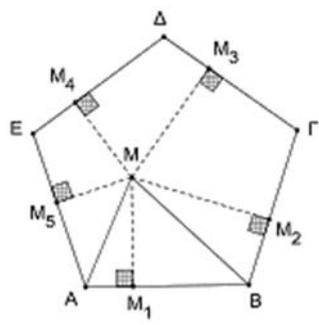
μ (,R).
) :
 i. Η μ
 ii. $\Gamma\hat{A}\Delta$ και $A\hat{\Delta}Z$.
 iii. μ
 iv. R μ
) μ μ μ μ
 μ ; μ μ μ μ



4 μ

22099.

M_1, M_2, M_3, M_4, M_5 μ , , , ,
) :
 i. $(ABM) = \frac{1}{2} \lambda_5 \cdot MM_1$, λ_5
 ii. $(AB\Gamma\Delta E) = \frac{1}{2} \lambda_5 \cdot (MM_1 + MM_2 + MM_3 + MM_4 + MM_5)$.
 iii. $MM_1 + MM_2 + MM_3 + MM_4 + MM_5 = 5\alpha_5$, α_5
 μ
) μ μ : « μ μ
 - 1 2... 1, 2,..., μ 1 2,
 2 3,..., 1 , $MM_1 + MM_2 + \dots + MM_v = v\alpha_v$. μ
 - ».

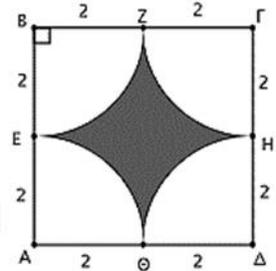


- ii. $\widehat{K\hat{A}\Lambda} = \hat{\omega}$, $\widehat{\Sigma\hat{B}P} = \hat{\omega}$, $\widehat{M\hat{\Gamma}N} = \hat{\phi}$, $\hat{\omega} + \hat{\theta} + \hat{\phi} = 360^\circ$.
) $L = 2(\tau + \pi R)$



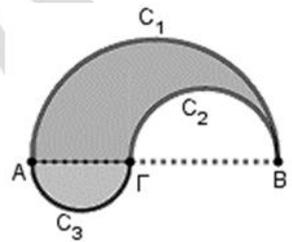
18098.

- $= 4$.
 $= 2$
) $= 4(4 -)$.



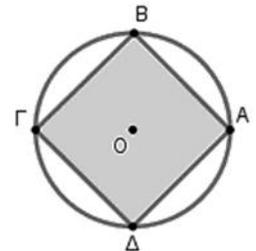
20672.

- $= 4$.
 C_1, C_2, C_3
) $\frac{9\pi}{2}, 2\pi$ και $\frac{\pi}{2}$
)



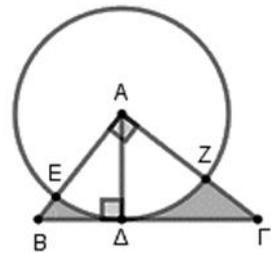
21075.

- μ , μ 16.
) 4 :
 i. $\mu\mu$
 ii. μ



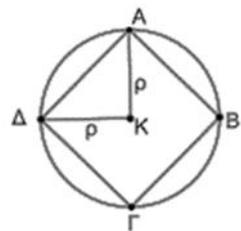
21121.

- $= 13$, $= 6$.
 μ , μ
) μ
) μ :
 i. μ $\widehat{AE\Delta Z}$,
 ii. μ



21300.

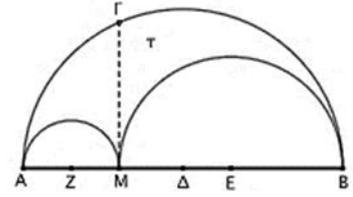
- $(,)$, μ .
) μ
) μ 4:
 i. $\rho = \sqrt{8}$.
 ii. μ $(,)$.



) ; μ μ μ μ μ . μ μ

22024.

$\mu\mu = 2$ $\mu\mu = 2$. μ μ , μ μ μ . μ μ μ

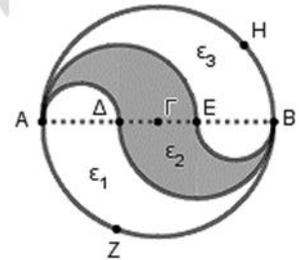


) \widehat{ZAM} , \widehat{EMB} και $\widehat{\Delta AB}$, , μ μ ,

) μ μ μ μ μ μ
 μ . μ μ μ μ μ μ
) μ μ μ μ μ μ μ μ
) μ μ μ μ μ μ μ μ ;

22058.

μ μ R. μ μ
 μ , μ = = . μ μ
 μ μ μ μ μ μ μ μ

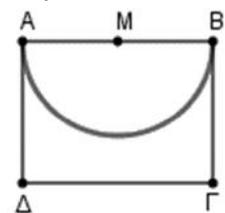


) μ 1 3 μ μ μ μ
) μ 2 μ μ μ μ
) μ μ μ μ μ μ μ μ .

22098.

μ μ = 4
 = . μ μ

) μ μ μ μ μ μ
) μ μ μ μ μ μ



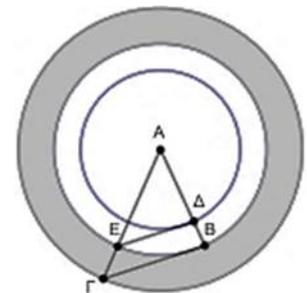
i. $AB^2 = B\Delta \cdot BE$ και $A\Delta^2 = B\Delta \cdot \Delta E$.

ii. $BE = \frac{16\alpha}{\sqrt{16+\pi^2}}$ και $\Delta E = \frac{\pi^2\alpha}{\sqrt{16+\pi^2}}$.

iii. $\sigma\upsilon\nu\widehat{BME}$.

22151.

μ < . μ μ
 μ μ = , r = = R = μ μ .
 μ (,) , (, r) (, R)
 (, r) (, R) , μ μ μ
 (,) (, r) , μ μ (, r) μ
 (,) . μ
) :



i. $\frac{E_{EF}}{E_{AE}} = \frac{R^2 - r^2}{r^2}$.

ii. $\frac{E_{AB}}{E_{AA}} = \frac{r^2 - \rho^2}{\rho^2}$.

) $\frac{E_{EF}}{E_{AE}} = \frac{E_{AB}}{E_{AA}}$.

22154.

(, 3), (, 1), (, 2)

μ , μ $1 < 2 < 3$. μ μ μ μ

) $\frac{E_{EF}}{E_2} = \frac{7}{9}$,

i. $\frac{\rho_2}{\rho_3} = \frac{3}{4}$.

ii. $\frac{E_2}{E_3} = \frac{9}{16}$.

iii.

$\frac{\rho_1}{\rho_2} = \frac{3}{4}$.

) $E_{EF} = E_2$

$E_{AB} = E_1$

22244.

10 m .

) 25 m^2 .

i. $50(\pi - 2)\text{ m}^2$.

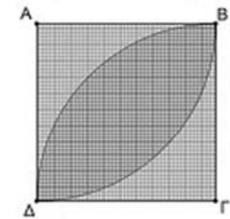
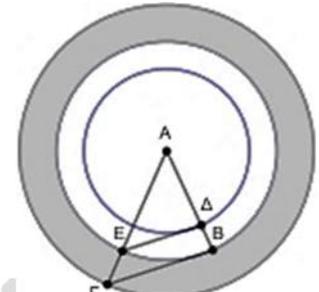
ii. 5 m .

i. 5 m .

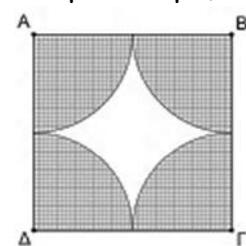
ii. 5 m .

5 m .

5 m .



Σχήμα 1



Σχήμα 2

22261.

$B\Gamma = \sqrt{\beta^2 + \gamma^2 + \beta\gamma}$.

) $\hat{A} > 90^\circ$.

) $\hat{A} = 120^\circ$. $\cos 120^\circ = -\frac{1}{2}$.

) $\hat{A} = 120^\circ$.

Ασκησότητα